NMU Math & CS Department Problem of the Month, November 2022

Suppose that $X \in \mathbb{C}$ is a number such that:

$$X^3 + \frac{1}{X^3} = \sqrt{2}.$$

Find the value of the expression:

$$X^{2022} + \frac{1}{X^{2022}} \,.$$