NMU Math & CS Department Problem of the Month, February 2023

Consider the number M = 11...111, with all of its n digits equal to 1.

For example: M = 111 when n = 3, M = 1111 when n = 4, and M = 11111 when n = 5.

Show that M is divisible by 41 if and only if n is divisible by 5.