

1. Simplify each expression

$$(a) \left(\frac{1}{-x}\right)^{-3}$$

$$(b) (-x)^4 - x^4$$

$$(c) \frac{x^{11}}{x^{12}} - \frac{x^{12}}{x^{11}}$$

$$(d) \frac{\sqrt[5]{yx^4}}{\sqrt{x^4}}$$

$$(f) \sqrt[4]{\frac{x^8}{y^{16}}}$$

$$(g) (x^4)^{-5/4}$$

2. Rationalize the denominator and simplify

$$(a) \frac{6}{\sqrt{x} + 1}$$

$$(b) \frac{6}{\sqrt{x}}$$

3. Simplify each expression, eliminating any negative exponents

(a)  $\sqrt{y^2x^3} - \sqrt{x}$

(b)  $(3a^3b^3)^2(2ab^2)$

(c)  $\sqrt[3]{\frac{27}{x^{-6}}}$

(d)  $\left(\frac{2x^{-3/4}y^3}{x^2y^{1/2}}\right)^{-4}$

4. Perform the indicated operations and simplify

(a)  $(x - y)^2 + x^2 - y^2$

(c)  $(\sqrt[3]{a} + \sqrt[3]{b})(\sqrt[3]{a} - \sqrt[3]{b})$

(d)  $(ab)^2 - a^2b^2 + \left(\frac{a}{b}\right)^2 - \frac{a^2}{b^2}$

5. Factor each expression completely

(a)  $25 - 9y^2$

(b)  $3x^2 + 7x - 20$

(c)  $x^6 + x^4 + x^2 + 1$

(d)  $(x^2 - 1)^{5/4}4x^{3/2} - x^{-1/2}(x^2 - 1)^{1/4}$

(f)  $x^3y^2 - 9xy$

6. Simplify the rational expression

$$(a) \frac{3}{2 - \frac{1}{x}}$$

$$(c) \frac{2}{x+1} - \frac{1}{x^2 - 9x - 10}$$

$$(d) \frac{\frac{y^2}{x} - \frac{x}{y^2}}{\frac{1}{y} - \frac{1}{x^2}}$$