

KEY

Name:

Quiz 1 :: Math 111 :: September 4, 2015

1. Simplify each expression, eliminating any negative exponents

(a)

$$(3a^3b^3)^2(2ab^2)$$

$$9a^6b^6 \cdot 2ab^2$$

$$\underline{18a^7b^8}$$

(b)

$$\sqrt[3]{\frac{27}{x^{-6}}}$$

$$= 3 \cdot (x^6)^{1/3} = 3x^2$$

$$\underline{3x^2}$$

(c)

$$\left(\frac{3x^{-3/2}y^3}{x^2y^{1/2}}\right)^{-2}$$

$$\left(\frac{x^2y^{1/2}x^{3/2}}{3y^3}\right)^2$$

$$\frac{x^4x^3y}{3y^6}$$

$$\underline{\frac{x^7}{3y^5}}$$

2. Perform the indicated operations and simplify

(a)

$$(x+y)^2 - x^2 - y^2$$

$$\underline{2xy}$$

(b)

$$(\sqrt{a} + \sqrt{b})(\sqrt{a} - \sqrt{b})$$

$$\underline{a - b}$$

(c)

$$\underbrace{(ab)^2 - a^2b^2}_{=0} + \left(\frac{a}{b}\right)^2 + \frac{a^2}{b^2}$$

$$\underline{\frac{2a^2}{b^2}}$$

(d)

$$\sqrt{4x^2 + 4y^2} - x - y$$

$$\underline{2\sqrt{x^2 + y^2} - x - y}$$

3. Factor each expression completely

(a) $36 - 9y^2$ $(6-3y)$ $(6+3y)$

(b) $3x^2 + 3x - 18$ $(3x + 9)(x - 2)$ $(3x+9)(x-2)$

(c) $x^5 + x^4 + x + 1$ $(x+1)(x^4+1)$

$x^4(x+1) + (x+1)$

(d) $3x(x+1)^{5/4} - x^2(x+1)^{1/4}$ $x(x+1)^{1/4} (3x+1-x)$ $x(x+1)^{1/4} (2x+1)$

(e) $x^3y - 4xy$ $xy(x^2-4)$ $xy(x-2)(x+2)$

4. Simplify the rational expression

(a) $\frac{x+1}{x+1} - \frac{1}{x+1}$ $\frac{3}{x+1}$ $\frac{3(x+1)}{x}$

(b) $\frac{x+4}{x+4} \cdot \frac{2}{x+3} - \frac{1}{x^2+7x+12} = \frac{2x+8-1}{x^2+7x+12}$

(c) $\frac{y^2}{y^2} - \frac{x}{y^2} \cdot \frac{1}{y} - \frac{1}{x}$ $\frac{y^4 - x^2}{xy^2}$ $\frac{y^4 - x^2}{y(x-y)}$

$\frac{x-y}{xy}$
