

• [euclid.nmu.edu/~rjoshtom/Teaching/MATH5](http://euclid.nmu.edu/~rjoshtom/Teaching/MATH5) - syllabus

Name:

Chapter P :: Real Numbers - Exponents, Radicals and Factoring :: Math 115

1. Set notation helps us communicate collections of numbers effectively. Find the indicated sets if

$$A = \{1, 3, 5, 7\}, B = \{2, 4, 6, 8\} \text{ and } C = \{7, 8, 9\}$$

union

(a)  $A \cup B = \text{in } A \text{ or } B = \{1, 2, 3, 4, 5, 6, 7, 8\}$

(b)  $A \cap B = \text{in } A \text{ and in } B = \emptyset \leftarrow \text{empty set}$

(c)  $B \cap C = \{8\}$

2. Find the indicated sets if

*such that*  
 $A = \{x \mid x < 4\} \text{ and } C = \{x \mid -1 < x \leq 6\} = (-1, 6]$

(a)  $A \cup C$

(b)  $A \cap C$

$\downarrow$  any real #  $x$   
 $= (-\infty, 4)$

3. The number line:

Graph the set  $(-2, 0) \cup (-1, 1)$

Graph the set  $[-4, 6) \cap [0, 8)$

PEMDAS =

4. Name the property illustrated:

$$2x + 5 = 5 + 2x \quad \text{commutative}$$

$$(2x + 5) + 7y = 2x + (5 + 7y) \quad \text{associative}$$

$$\begin{aligned} 30 & \\ \text{"} & \\ 3(10) & = 3(8+2) = 3 \cdot 8 + 3 \cdot 2 \end{aligned}$$

$$A(C + D) = AC + AD \quad \text{distributive} \leftarrow$$

5. Is this true or false?  $(A + B)(C + D) = (A + B)C + (A + B)D$

$$A + B = E$$

"

$$E(C + D) = EC + ED$$

6. Simplify into one power of two.  $4^x \cdot 2^y = 2^{\quad}$

$$4^x \cdot 2^y = 2^{\quad}$$

||

$$[2^2]^x \cdot 2^y = 2^{2x} \cdot 2^y = 2^{2x+y}$$

7. Simplify  $(2^2)^5$

8. Simplify  $(y+x)^3(y+x)^{-5}$

$$(y+x)^3 \cdot \frac{1}{(y+x)^5} = \frac{(y+x)^3}{(y+x)^5} = \frac{1}{(y+x)^2}$$

Annotations:  $3+(-5)$  above the first  $(y+x)$  term,  $(y+x)^{-2}$  above the second  $(y+x)$  term, and arrows pointing from the exponents to the simplified denominator.

9. Simplify  $\left(\frac{xy}{4}\right)^3 \left(\frac{2x^2}{4y}\right)^5$

key  
mult. like bases  $\Rightarrow$  add exponents  
 $A^m \cdot A^n = A^{m+n}$   
raise a power to a power  
 $\Rightarrow$  multi. powers  
 $(A^m)^n = A^{m \cdot n}$

8.  $4 = 32$

$$2^3 \cdot 2^2 = 2^5 = 2^{3+2}$$
$$(2^3)^2 = 2^3 \cdot 2^3 = 2^{3+3} = 2^{2 \cdot 3}$$