

Thursday - Week 5

warm-up:

- ① Give a degree 3 poly. with zeros $-1, 3, 7$ that passes through $(0, 5)$

$$f(x) = Ax^3 + Bx^2 + Cx + D$$

$$= A(x - (-1))(x - 3)(x - 7) = A(x + 1)(x^2 - 10x + 21)$$

$$= A(x^3 - 10x^2 + 21x + x^2 - 10x + 21)$$

$$= A(x^3 - 9x^2 + 11x + 21)$$

$$= \frac{5}{21}(x^3 - 9x^2 + 11x + 21)$$

Also

$$f(0) = 5 = A(0^3 - 0^2 + 0 + 21)$$

$$= 21A$$

$$A = \frac{5}{21}$$

- ② Give a rational function that has:

- Horizontal Asy @ $y = 3$
- Vertical Asymptotes @ $x = 5, x = -2$

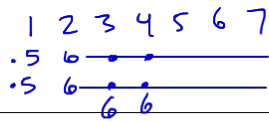
Q

Can you give lots more examples w/ same criteria?

$$\frac{3}{1 \cdot (x - 5)(x + 2)}$$

← has specified V. Asy
but Horiz Asy is $y = 0$

$$\frac{3x^2 + x}{(x - 5)(x + 2)}$$



Something like this will appear on subsequent exams

1. Simplify the expression:

(a) $4x^3(2x^0)^{-4} = 4x^3 \cdot \frac{1}{2^4} = 4 \cdot \frac{x^3}{16} = \frac{x^3}{4}$

$(2 \cdot 1)^{-4}$

$2^{-4} = \frac{1}{2^4}$ $3^2 \cdot x^{-2}$
 $3 \cdot 3 \cdot x^{-1} \cdot x^{-1}$

(b) $\frac{(3x^{-1})^2 y^4 z^8}{3xy^7 z^0} = 3x^{-1} \cdot 3x^{-1}$

$$\frac{3x^{-2} z^8}{3x y^7 y^{-4}} = \frac{3z^8}{x^3 y^3}$$

2. Completely factor the polynomial:

(a) $x^3 - 5x^2 - 9x + 45$

$$\begin{aligned} &x^2(x-5) - 9(x-5) \\ &(x^2 - 9)(x-5) \\ &(x-3)(x+3)(x-5) \end{aligned}$$

AC: $3(-8) = -24$

$1, 2, 3, 4, 6, 12, 24$ $3x^2 - 12x + 2x - 8$

$3x(x-4) + 2(x-4)$

$(3x+2)(x-4)$

3. Find all solutions to the equations:

(a) $x^4 - 8x^2 + 16 = 0$

set: $w = x^2$

so $w^2 = x^4$

sub: $w^2 - 8w + 16 = (w - 4)^2 = 0$

$w = 4$

back
sub

$x^2 = 4$

$x = \pm 2$

(b) $(\sqrt[3]{x-7} + 4) = 0$

Wrong ↓

$x-7 + 4^3$

RIGHT

isolate radical

$\sqrt[3]{x-7} = -4$

$x-7 = -64$

$x = -57$

(c) $x - 4 = \sqrt{2x}$

$(x-4)^2 = 2x$

$x^2 - 8x + 16 = 2x$

$x^2 - 10x + 16 = 0$

$(x-8)(x-2) = 0$

$x = 8$

$x = 2$

4. Find the Domain of the functions:

↳ set of allowable inputs

(a) $f(x) = 5x^2 + 19x - 12$

— poly —

\mathbb{R}

(b) $g(x) = \sqrt{6-x}$

$6-x \geq 0$

$(-\infty, 6]$

(c) $q(x) = \frac{3x}{9x^2 - 81}$

(cancel ÷ by 9)

$9x^2 - 81 = 0$

$9(x^2 - 9) = 0$

$x^2 - 9 = 0$

$x = \pm 3$

$\mathbb{R} - \{\pm 3\}$

5. Find the following composition of:

$f(x) = 2x + 6$

$g(x) = x^2 - 3x + 12$

(a) Find the function $g \circ f$

(b) Find the function $f \circ f$

6. Write an equation for the line that satisfies the following characteristics:

(a) passes through points $(-3, -2)$ and $(6, 10)$

(b) passes through the point $(5, -2)$ and has an undefined slope

vertical line
(all x's are constant)

$$x = 5$$

(c) passes through $(8, -1)$ and perpendicular to $6x - 3y - 5 = 0$

↓ extract slope

$$6x - 5 = 3y$$

$$= y$$

7. Find the inverse of the following functions:

(a) $f(x) = \sqrt{2x - 13}$

(b) $f(x) = \frac{4x - 3}{-x + 5}$