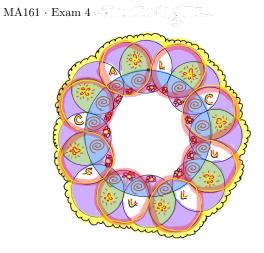
Applications ______

1. Evaluate the limit (a)

$$\lim_{x \to 0^+} \frac{2x^4 - 8x^2}{x^4 + 4x^2} = \frac{0}{0}$$

$$= \lim_{x \to 0} \frac{x^2(2x^2 - 8)}{x^3(x^2 + 4)} = \lim_{x \to 0^+} \frac{2x^2 - 8}{x^2 + 4}$$
$$= -2$$



(b)

$$\lim_{x \to 0} \frac{\sin x - x}{x^3} \quad = \quad \stackrel{\mathsf{O}}{\longrightarrow}$$

L'Hopitals

$$= \lim_{X \to 0} \frac{\cos x - i}{3x^2} = \frac{0}{0}$$
L'H

$$= \lim_{X \to 0} \frac{-\sin x}{6x} = \frac{0}{0}$$

$$\begin{array}{ccc} L'H \\ = \\ \chi - 90 \\ \hline 6 \\ \hline 6 \\ \hline 6 \\ \hline 6 \\ \hline \end{array} = \begin{pmatrix} -1 \\ -1 \\ \hline 6 \\ \hline 6 \\ \hline \end{array}$$

2. Find the point on the line $y = \sqrt{x+1}$ that is closest to the point (8,0).

$$\mathcal{M}_{\text{inimize distance function from } y = \sqrt{x+1} \quad \text{to } (8,0)$$

$$d(x) = \sqrt{(8-x)^2 + (0 - \sqrt{x+1})^2}$$

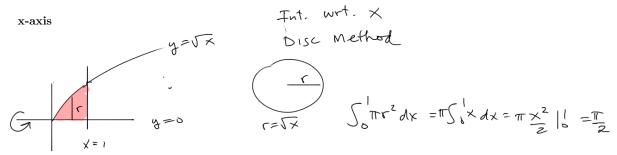
$$= \sqrt{(64 - 16x + x^2) + (x+1)}$$

$$= \sqrt{x^2 - 15x + 65}$$

$$d(x) = \frac{1}{2}(x^2 - 15x + 65)^{-1/2}(2x - 15) = 0$$

$$\Rightarrow 2x - 15 = 0 \quad x = 7.5 \quad \text{As } = 7$$

3. Consider the region bound by $\neq 0$ and $y = \sqrt{x}$. Find the volume of the solid of revolution when the region is revolved about the:



4. Revolve the region above about the **y-axis** and compute the volume of the resulting solid.

$$\frac{shell Method}{(ntegrate wrt x)}$$

$$r = x$$

$$h = \sqrt{x}$$

$$\int_{x=1}^{1} 2\pi x \sqrt{x} dx = 2\pi \int_{x}^{3/2} dx$$

$$= \frac{2!}{5} 2\pi x \sqrt{x} dx = \frac{2\pi}{5}$$

5. Suppose the volume of a spherical balloon increases at a rate of $24 \frac{cm^3}{sec}$. Find the rate that its diameter is - increasing when the diameter is 3cm.

$$V = \frac{4}{3}\pi r^{2}$$

$$\frac{dV}{dt} = 4\pi r^{2} \cdot \frac{dr}{dt} = 24$$

$$\frac{dv}{dt} = \frac{24}{4\pi r^{2}} \cdot \frac{dr}{dt} = 24$$

$$\frac{dv}{dt} = \frac{24}{4\pi r^{2}} \cdot \frac{dr}{dt} = \frac{24}{3\pi r^{3}} \cdot \frac{dr}{s}$$

$$= \frac{24}{\pi \cdot 4 \cdot \frac{q}{4}} = \frac{8}{3\pi} \cdot \frac{cm}{s}$$

$$= \frac{24}{\pi \cdot 4 \cdot \frac{q}{4}} = \frac{8}{3\pi} \cdot \frac{cm}{s}$$

$$= \frac{16}{3\pi} \cdot \frac{cm}{s} = \frac{16}{3\pi} \cdot \frac{cm}{s} = \frac{16}{3\pi} \cdot \frac{cm}{s}$$

6. Find the absolute maximum and absolute minimum of the function on the indicated interval.

$$f(x) = \frac{x^4}{4} - 2x^2 + 1, \ [-3,1]$$

7. A gardener is planning to build a rectangular fence which encloses 28 ft². One of the sides is to be made of stone which costs $10\frac{\$}{ft}$, and the remaining sides are to be made of wood which costs $4\frac{\$}{ft}$. (a) What dimensions minimize the cost of such a fence? (a) What dimensions minimize the cost of such a fence?<math>(a) What dimensions minimize the cost of such a fence?

$$C_{\text{inerv}}: A = 28$$

$$cost \text{ of store}: \frac{5}{0}/4t \qquad \frac{10}{10} \cdot \omega + \frac{5}{4} \cdot 1 + \frac{5}{4} \cdot \omega + \frac{5}{4} \cdot 4 \\ cost \text{ of wood}: \frac{5}{4} \cdot \frac{7}{0}/4t \qquad \frac{10}{4} \cdot \frac{5}{4} \cdot \frac{10}{4} + \frac{10$$

(b) What is the minimum cost?

$$C(w) = 14\left(4 + \frac{1b}{4}\right) = 14\left(8\right) = 14\left(8\right)$$

Minimize Cost :

$$C'(w) = 14\left(1 - \frac{16}{w^2}\right) = 0$$

$$= \frac{16}{w^2} \quad \text{we } = \frac{4}{\sqrt{y^2}}$$

$$e \quad l = \frac{28}{\sqrt{y}} = 7$$

8. A boat leaves Marquette at 3:00 PM and travels due north at a speed of 10 m/h. Another boat has been heading west at 15 m/h and reaches Marquette at 5:00 PM. At what time were the boats closest together?

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$$(d^{2})' = 2(10t) \cdot 10 + 2(-15t + 30)(-15) = 0$$

$$= 2(10t) - 3(-15t + 30) = -0$$

$$= 20t + 45t - 90 = 0$$

$$= 20t + 90 = 0$$

$$= 20t +$$

9. A fence 7 feet tall runs parallel to a tall building at a distance of 6 feet from the building. What is the length of the shortest ladder that will reach from the ground over the fence to the wall of the building?

$$\frac{1}{x} = \frac{1}{x} + \frac{1}$$

10. A box with an open top is to be constructed from a square piece of cardboard, 6 ft wide, by cutting out a square from each of the four corners and bending up the sides. Find the largest volume that such a box can have.

× V=liwin w=l=
$$(p-2x)$$
 where $x = length$ of cut
 $V = x (b-3x)^{3}$
 $V' = (.(b-3x)^{3} + x.3(b-3x)(-3))$
 $= (b-3x)(b-3x) - 4x = 0$
 $= (b-3x)(b-6x) = 0$
 $x=3$ or $x=1$
(exclude (two big))
 $V = 1(b-3(1))^{3} = (1b + 3)$

11. Find the equation of the tangent line to the graph of $y = (x^2 + 1) \sin x$ at x = 0.

slope
$$y' = 3x \cdot 8m\chi + (x^{2}+1)\cos x$$

 $y'(o) = 1$
 $x_{1} = 0$
 $y_{1} = .0$
 $(y = \chi)$