## Exam 1

Show all work to receive credit. Access to internet / graphing calculator / etc during the exam will result in a score of 0 .
1.
$\int x^{3} \cos (2 x) d x=$
2.
$\int \frac{2 x+1}{(x-2)(x-6)} d x=$
3.
$\int x^{3} \sin ^{2}\left(x^{4}\right) d x=$
4.
$\int \tan ^{3} \theta \sec ^{3} \theta d \theta=$
5.
$\int x^{3} \sqrt{x^{2}+4} d x=$
6. (you need to do at least three of the following; additional ones may be done for extra credit.)
Evaluate at least three of the following integrals:
(a)

$$
\int 2 x \tan ^{-1} x d x=
$$

(c)

$$
\int \frac{\sqrt{x^{2}-9}}{x^{4}} d x=
$$

(d)

$$
\int e^{3 x} \sin 4 x d x=
$$

(e)

$$
\int \frac{x^{2}}{\sqrt{16-x^{2}}} d x=
$$

(f)

$$
\int \frac{x^{2}+4 x+6}{x\left(x^{2}+2 x+1\right)} d x=
$$

Scratch work

Scratch work

$$
\begin{gathered}
\sin 2 x=2 \sin x \cos x \\
\cos 2 x=\cos ^{2} x-\sin ^{2} x
\end{gathered}
$$

$$
\begin{aligned}
& \cos ^{2} \theta=\left(\frac{1}{2}\right)(1+\cos 2 \theta) \\
& \sin ^{2} \theta=\left(\frac{1}{2}\right)(1-\cos 2 \theta)
\end{aligned}
$$

$$
\begin{aligned}
\sin A \cos B & =\frac{1}{2} \sin (A-B)+\frac{1}{2} \sin (A+B) \\
\sin A \sin B & =\frac{1}{2} \cos (A-B)-\frac{1}{2} \cos (A+B) \\
\cos A \cos B & =\frac{1}{2} \cos (A-B)+\frac{1}{2} \cos (A+B)
\end{aligned}
$$

