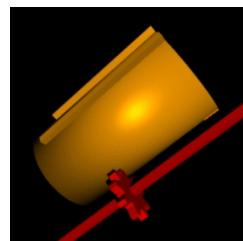


Leibniz's calculator



Leibniz wheel



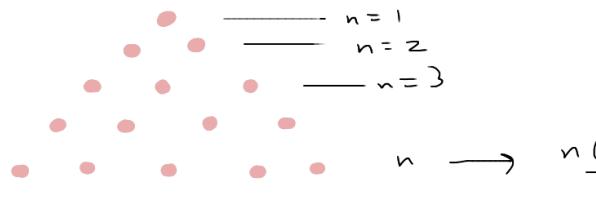
Popular Handheld Calculator

Leibniz's Formal Logic

1. All our ideas are compounded from a very small number of simple ideas, which form the **alphabet of human thought**.
2. Complex ideas proceed from these simple ideas by a uniform and symmetrical combination, analogous to arithmetical multiplication.

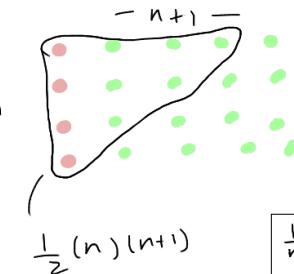
TRIANGULAR #'S

$$\frac{n(n+1)}{2}$$



Liebniz Proved:

$$1 + \frac{1}{3} + \frac{1}{6} + \frac{1}{10} + \dots + \frac{1}{\frac{n(n+1)}{2}} + \dots = \infty$$



$$\begin{aligned} & \frac{1}{n} - \frac{1}{n+1} \\ & \frac{n+1}{(n+1)n} - \frac{n}{(n+1)n} \\ & \frac{1}{n(n+1)} \end{aligned}$$

$$S = 1 + \frac{1}{2} + \frac{1}{3} + \frac{1}{4} + \frac{1}{5} + \frac{1}{6} + \dots + \frac{1}{n} + \frac{1}{n+1}$$

$$-S = -1 - \frac{1}{2} - \frac{1}{3} - \frac{1}{4} - \frac{1}{5} - \frac{1}{6} - \dots - \frac{1}{n} - \frac{1}{n+1}$$

$$0 = -1 + \frac{1}{2} + \frac{1}{6} + \frac{1}{12} + \frac{1}{20} + \frac{1}{30} + \dots + \frac{1}{n(n+1)} + \frac{1}{n+1}$$

$$1 - \frac{1}{n+1} = \frac{1}{2} + \frac{1}{6} + \frac{1}{12} + \frac{1}{20} + \frac{1}{30} + \dots + \frac{1}{n(n+1)}$$

Take $\lim_{n \rightarrow \infty}$

$$1 = \frac{1}{2} + \frac{1}{6} + \frac{1}{12} + \frac{1}{20} + \frac{1}{30} + \dots$$

∴ multiply by 2

$$2 = 1 + \frac{1}{3} + \frac{1}{6} + \frac{1}{10} + \frac{1}{15} + \dots \text{ sum of recip of } \Delta \text{ #'s Liebniz's Series.}$$