Wednesday

▼1. Archimedes: 225 BC

▼a. Works

- ▼i. On the Measurement of a Circle
 - **v1.** Showed how to calculate the area of a circle
 - a. by relating it to a triangle
 - **v2.** Estimated pi (well) by exhaustion
 - ▼a. It had been estimated before his time: I Kings 7:23
 - i. "Then He made the molten sea, then cubits from brim to brim, while a line of 30 cubits measured it round."

▼ii. On the Sphere & Cylinder

- **v1.** Computed areas of spheres / cones / cylinders
 - a. by exhaustion, filling up spheres with cones & frustrums
- 2. Related the sphere to the cylinder in interesting way
- **3.** Related the volume constant, the area constant, the length constants ... all to what would be known as pi
- **74.** Prop. 13 The surface of any right circular cylinder excluding bases is equal to a circle whose radius is a a mean proportional between the side of the cylinder and the diameter of the base.
 - **Ta.** Explain "mean proportional" b/w side of cylinder and diameter. let h = side of cylinder, 2r = diameter, the mean proportional is x where h/x = x/(2r).
 - i. Thus $x^2 = 2hr$ and the radius is x. Thus the area of the open cylinder is the same as the area of the circle with radius x. We know this to be pi * x^2 thus 2*pi*r*h

5.

- Pi
 - 1. Egypt Rhind Papyrus (4/3)^4 = 3.160..
- ▼2. Bible: I Kings 7:23
 - a. "Then He made the molten sea, ten cubits from brim to brim, while a line of 30 cubits measured it around."
- ▼ 3. In the 2nd century CE, Ptolemy used the value ³⁷⁷/₁₂₀, the first known approximation accurate to three decimal places. It is equal to 3 + 8/60 + 30/60^2
 - ▼a. table of chords
 - i. the chord of 1 degree is 1.0472 p where the diameter is 120 p
 - ii. multiplying the above by 360 gives the circumference: 376.992p or pi = 3.1416
- ▼4. Chinese: 150 AD

a. The Chinese mathematician Liu Hui in 263 CE computed π to between 3.141024 and 3.142708 by inscribing a 96-gon and 192-gon;

- 5. Bhaskara (1110 CE) ... pi = 3.1416
- 6. Simon Stevin (1500 CE) decimal system, helped matters
- ▼7. Francois Viete: (1550 CE)
 - ▼ a. used polygons with 393,216 sides ... 9 decimal places.
 - i. doubling Archimedes another 12 times!
 - ▼b. Ludolph van Ceulen (1600's)
 - i. 35 correct decimal places
 - ii. after years of effort
 - iii. polygon with 2^62 sides. (4 million trillion sides)

▼c. Leibniz's series: 1 - 1/3 + 1/5 - 1/7 + 1/9 - 1/11 + 1/13 - 1/15 + ... approximates pi/4

- i. from geometry to arithmetic
- ii. approaches slowly
- iii. after 150 terms only get 3.1349
- iv. little practical use
- d. Shart (1650) 71 places, Machin (1680) 100 places
- e. Lambert (1750) pi is irrational, so none decimal is gonna get it.
- ▼8. Ramanujan (1887-1920)
 - a. poor, self taught, failed out of school,
 - b. was urged to write of his discoveries to England, one sent to G.H. Hardy (Cambridge) (1913)
 - ▼c. strange formulas, poor English ... it haunted Hardy all day
 - i. "the formulas must be true bc no one has the imagination to invent them.
 - d. travel to England was hard due to religion, diet, but he arrived in Cambridge 1914.
 - e. Highly accurate approximations to pi
 - f. 1919, back to India in poor health.
 - ▼g. Story of Ramanujan on death bed

The number 1729 is known as the Hardy–Ramanujan number after a famous visit by Hardy to see Ramanujan at a hospital. In Hardy's words:^[76]

I remember once going to see him when he was ill at Putney. I had ridden in taxi cab number 1729 and remarked that the number seemed to me rather a dull one, and that I hoped it was not an unfavorable omen. "No", he replied, "it is a very interesting number; it is the smallest number expressible as the sum of two cubes in two different ways."

i.

Immediately before this anecdote, Hardy quoted Littlewood as saying, "Every positive integer was one of [Ramanujan's] personal friends."^[77]

The two different ways are:

 $1729 = 1^3 + 12^3 = 9^3 + 10^3.$

h. Formula for pi

The Classical Mathematicians -- And Beyond -See: table of contents

- // //Agriculture -Moscow Papyrus First Humans 1850 BC to Americas Plimpton 322 15,000 BC

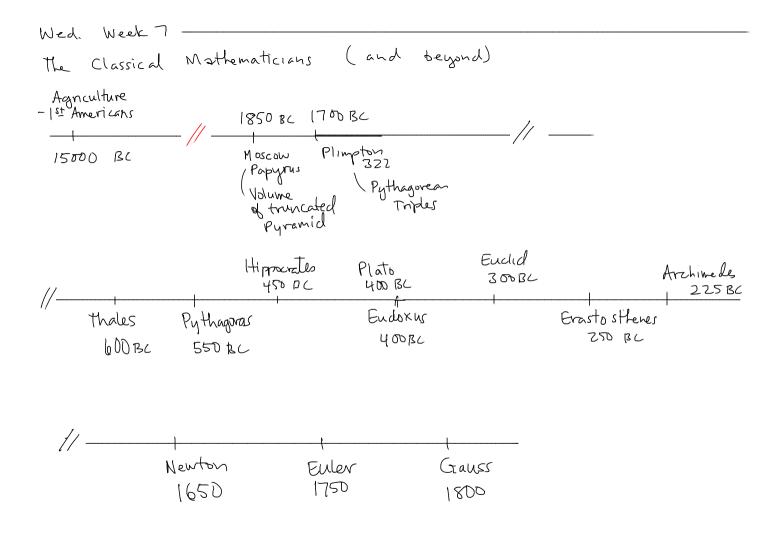
1700 BC

Hippocrates Erastosthenes Thales Plato 450 BC 250 BC 600 BC 400 BC - // Archimedes Pythagoras Euclid Eudoxus 225 BC 550 BC 400 BC 300 BC Euler 1750 // Newton Gauss 1650 1800

The Classical Mathematicians -- And Beyond -See: table of contents

____ // // Agriculture -Moscow Papyrus (volume of frustum 1850 BC of pyramid) First Humans to Americas Plimpton 322 (pythas, triples) 15,000 BC 1700 BC

	Thales	Plato		Hippocrates		Erastosthenes		
// -	600 BC	400 BC		450 BC		250 BC		//
//	Pythag	joras	Eudoxus		Euclid		Archimedes	//
	550 BC	0	400 BC		300 BC		225 BC	
					Euler			
			//		1750			
_			//	Newton		Gauss		
				1650		1800		



$$\frac{1}{\pi} = \sum_{n=0}^{\infty} {\binom{2n}{n}}^{3} \frac{42n+5}{2^{12n+4}}.$$

$$\binom{P}{q} = \frac{P!}{q!(P-q)!}$$
Binomial Coef
$$\binom{1}{1} \frac{1}{2} \frac{1}{1} \frac{1}{2}$$

$$\binom{S}{1} \frac{1}{4} \frac{1}{6} \frac{1}{4} \frac{1}{4} \frac{1}{4}$$

$$\binom{S}{1} \frac{S}{1} \frac{$$

$$\begin{pmatrix} 2n \\ n \end{pmatrix} = 7$$

Leibniz!
$$\frac{11}{4} = 1 - \frac{1}{3} + \frac{1}{5} - \frac{1}{7} + \frac{1}{9} - \frac{1}{11} + \frac{1}{13} - \frac{1}{11}$$

(while easy - it's slow!)
after 150 terms! we're only accurate to 3.1349

$$Rcmanujan:$$

 $1729 = Rancunyz - Hardy Number -$
 $= 1^{3} + 12^{3} = 9^{3} + 10^{3}$

On
$$\pi$$

Phind Papymo : $(\frac{4}{3})^4 = 3.16$ (earliest approx to π)
(1700 BC)
I Kings 7:23 V ($\pi \approx 3$)
Ludsliph van (eulen (1600's)
. π - connect to 35 decimal places
. π - connect to 35 decimal places
. method of Exhaustron ; # of sides of polygon = 3^6
Y million trillion sides