

75 AD

→ 1545

Classical Mathematics After Archimedes:

- Syracuse fell to the Romans (212 BC)
 - Carthage fell 146 BC
 - Caesar conquered 49 BC
 - Anthony & Cleopatra fell to Octavia in 30 BC
- } Roman Empire Begins

Ancient Romans were a practical ^{engineering} people who did not have a taste for pure mathematics.

- No great Roman Mathematician mentioned in Dunham.

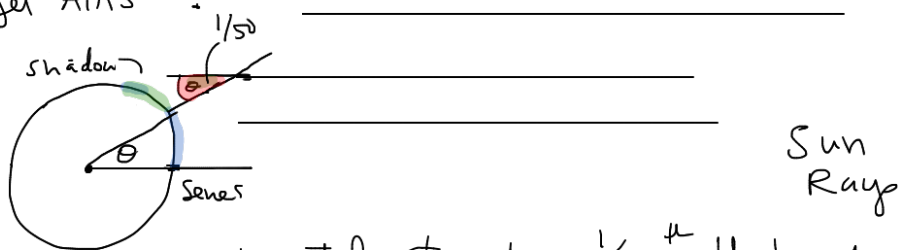
Library at Alexandria:

- Romans eventually control (30 BC) many of the scholars there were forced to evacuate. They did, & spread knowledge teaching.

Eratosthenes (284-197 BC)

- Machine
- Sieve for finding primes (Dunham)
- Accurate measure of circumference of the Earth.

B/C parallel, get AIA's =



1. Angle θ was estimated to be $1/50^{\text{th}}$ that of a full revolution

2. How far from Syene to Syracuse? 5000 "stadia"

(stadium
516.73' = 1 stadia

So: $\frac{5000}{\text{Circumference}} = \frac{1/50}{1}$

Circumf = $5000 \times 50 = 250000$ stades
 $\approx 24,466$ miles

24,860
"actual"

During the Roman rule,

- Mathematical progress was slow
- classical works of Euclid, et al were kept by the Arabians. (Baghdad)
- The Muslim inhabitants studied these classics.
- One bit of progress: Hindu-Arabic numeral system.
BTW - The mathematics of India during this period 0-1000 CE was superior to European Mathematics
- Al-Khwarizmi - Al'jbr. (although no symbol manipulation there was verbal descriptions of solving algebraic problems)
400 CE (beginning of algebra)

- Crusades: Attempted Christian Conquest of Middle East (11-13th Century)

Christian Conquest

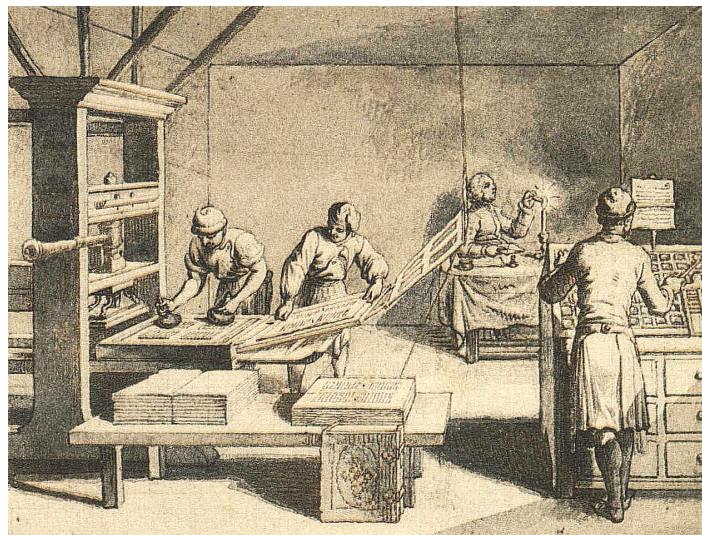
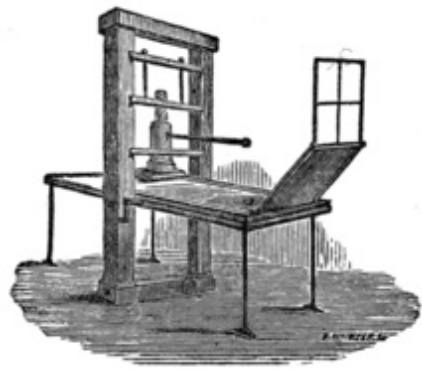
- Moors: _____ (Spain / Sicily)
_____ found classical works.
_____ this began the Renaissance.



[Medieval university](#) class (1350s)



1440



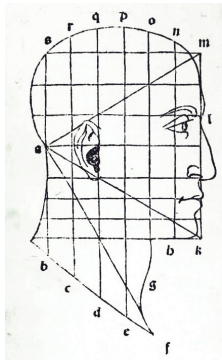
Renaissance

3600 pages per day

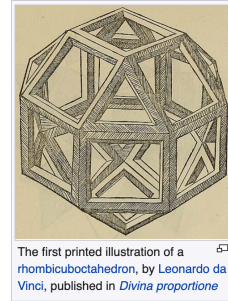




1492



Luca Pacioli
1494



- Luca Pacioli**
- ▼ 1. Published *Divina Proportione*
 - a. On math / perspective / golden ratio
 - b. Da Vinci made the illustrations
 - ▼ 2. Published *Summa de Arithmetica*
 - a. solve linear/quadratics
 - b. primitive symbolic algebra: *co = cosa = thing*
 - 3. Wrote: the general cubic equation is unsolvable

$$ax^2 + bx + c = 0 \quad (\text{quadratic formula})$$

$$ax^3 + bx^2 + cx + d = 0$$

similar?

$$x = \sqrt[3]{\left(\frac{-b^3}{27a^3} + \frac{bc}{6a^2} - \frac{d}{2a}\right) + \sqrt{\left(\frac{-b^3}{27a^3} + \frac{bc}{6a^2} - \frac{d}{2a}\right)^2 + \left(\frac{c}{3a} - \frac{b^2}{9a^2}\right)^3}} + \sqrt[3]{\left(\frac{-b^3}{27a^3} + \frac{bc}{6a^2} - \frac{d}{2a}\right) - \sqrt{\left(\frac{-b^3}{27a^3} + \frac{bc}{6a^2} - \frac{d}{2a}\right)^2 + \left(\frac{c}{3a} - \frac{b^2}{9a^2}\right)^3}} - \frac{b}{3a}$$



Leonardo da Vinci's failed attempt to solve $x^3 = 2$



$$7x^3 + 5x = 5$$

Scipione del Ferro
Born: 1465

del Ferro

- ▼ 1. Father worked in paper industry
 - a. Possible b/c printing press
 - b. This likely gave del Ferro access
- ▼ 2. Depressed Cubic: Cube and cosa equals number
 - a. Solved it!
 - ▼ b. Didn't tell
 - i. Save the solution for challenges
- ▼ 3. Daughter married a mathematician
 - a. undoubtedly knew of Scipione's solution
- 4. On deathbed, told his student, Antonio Fior

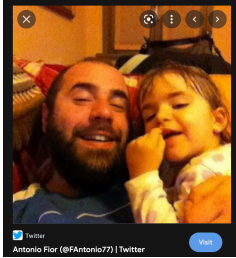
$$ax^3 + bx^2 + cx + d = 0$$

↓ depressed

$$ax^3 + cx = d$$

Antonio Fior

1. Student of del Ferro
- ▼ 2. Challenged Niccolo Fontana (b. 1500) to a duel
 - a. armed with ONLY the solution of the depressed cubic

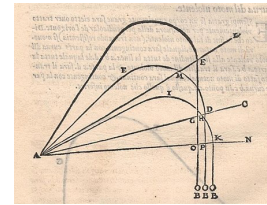
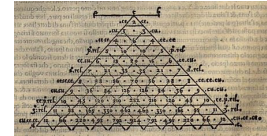


$$x^3 + mx = n$$



Niccolò Fontana Tartaglia: Italy 1500 - 1557

"stammerer"



Tartaglia

1. Powerful mathematician
2. 1st Italian translations of Euclid & Archimedes (1st correct Europea version of Elements)
3. Studied ballistics
4. Tartaglia eked out a living teaching practical mathematics in [abacus schools](#) and earned a penny where he could:

"This remarkable man was a self educated mathematics teacher who sold mathematical advice to gunners and architects, ten pennies one question, and had to litigate with his customers when they gave him a worn out cloak for his lectures on Euclid instead of the payment agreed on."



Begged Tartaglia for the solution



Pacioli: 1450



Scipione del Ferro: 1465

?

Antonio Fior: 1506



Niccolò Fontana Tartaglia: Italy 1500 - 1557



solved depressed cubic
- told no one (only Fior)
(son in law
was Mathematizer)

1st Italian
translation
of Euclid
and Archimedes

- also (independently)
solved depressed cubic
- didn't want to share, eventually did — in 4 poems
— forced Cardano not to share.

- wild man
- begged Tartaglia for
depressed cubic sol'n.
- eventually has student
↳ they travel to library
where they find
Del Ferro's Sol'n
(son-in law)
- Felt he was 'off the
hook' on sharing.