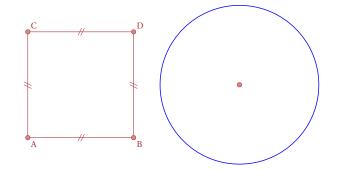
Study Guide:
 MA495 Exam 2 April 19, 2020

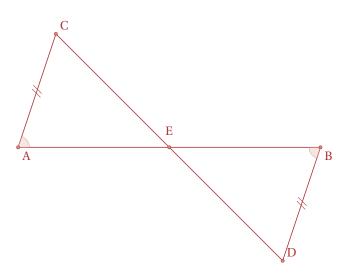
1. Note: P-model refers to the Poincaré model which is the usual (Euclidean) unit disk in \mathbb{R}^2 .

I Computations in Hyperbolic Geometry

- 1. Briefly explain why the Incidence & Betweenness Axioms hold in the Poincaré Model.
- 2. Sketch the inversion of the square below about the circle.



- 3. Breifly describe how inversions and rotations can be used to show that SAS congruence holds in hyperbolic geometry. (Work in the Poincaré model.)
- 4. One way to construct the midpoint of a segment AB in Euclidean geometry is to choose a point C on one side of AB, mark of the angle ∠CAB and then form the congruent ∠ABD on the other side of the line AB as shown. The line CD then bisects AB. (Why?) Apply this same argument to hyperbolic geometry as follows:



(a) Let AB be a P-segment in the P-model. Show how to construct its midpoint.

- (b) Show how to find the perpendicular bisector of a segment in the P-model. By the preceding problem, all that remains is to describe how to find the perpendicular P-line to AB through a point M.
- 5. Show how to find the P-angle bisector of an angle in the P-model.
- 6. How does one construct the center of P-circle in the P-model?
- 7. Draw a picture in the P-model which describes Exercise 8, p. 272, and Exercise 9, p. 273.
- 8. Let $(x_1, y_1) = (-0.85663050725, -0.515930396354)$ and $(x_2, y_2) = (-0.026468 0.999)$.
 - (a) Find the Euclidean distance between (x_1, y_1) and (x_2, y_2) .
 - (b) Find the Poincaré distance between (x_1, y_1) and (x_2, y_2) .
- 9. Describe how to find the P-line through points P and Q in the P-model.
- 10. What must be true if δ is a circle, R is an inverson about circle γ and R(δ) = δ ? Intuitively, why must this be?
- 11. Is hyperbolic geometry consistent?
- 12. Does the existence of multiple lines through a single point which are all parallel to a given line suggest anything philosophically interesting to you?