Math 163 - Calculus - Exam 2 - Guide

Name:

Show your work to receive full credit.

- 1. In each of the following, determine convergence/divergence. Indicate which test(s) you are using.
 - (1.1) Indicate absolute convergence, conditional convergence or divergence

$$\sum_{k=0}^{\infty} \frac{(-1)^n}{2n} \qquad \text{Alternating} \qquad \sum_{k=0}^{\infty} \frac{(-1)^n}{2n} \qquad \text{By AST} \Rightarrow \text{Senics}$$
 converges

$$\left| \frac{(-1)^n}{2n} \right| = \left| \frac{1}{2} \left(\frac{1}{2} \right) \right| = \left| \frac{1}{2} \left$$

$$(1.2) \sum_{k=2}^{\infty} \frac{2k\sqrt[3]{k}}{3k^2 + 5k + 1}$$
 L.C.T. w/ $\frac{2k\sqrt[3]{k}}{3k^2} = \frac{2}{3k^2/3}$ /

$$\frac{2k}{3k^2+5k+1} \cdot \frac{3k^3}{2} = \lim_{6k^2+5k+1} \frac{6k^2}{6k^2+5k+1} = 1 \implies \text{basically Same}$$
Sequences

since
$$\sum_{3k^{2/3}}^{2}$$
 diverges (p-test)

this series diverges

$$(1.3) \sum_{k=1}^{\infty} \cos\left(\frac{1}{k^2}\right)$$

LICT
$$\frac{\cos\left(\frac{1}{k^2}\right)}{\frac{1}{k^2}} = \lim_{n \to 0} \frac{\cos(n)}{n} = \frac{1}{0} \to \infty \Rightarrow ?$$

$$(1.4) \sum_{k=1}^{\infty} \left[\frac{8}{5} - \frac{\sqrt[k]{5}}{2} \right]^{k}$$

$$\text{Root}$$

$$\text{Lin} \left(\frac{3}{5} - \frac{\sqrt{5}}{2} \right)^{k} = \text{Lin} \frac{3}{5} - \frac{\sqrt{5}}{2} = \frac{8}{5} - \frac{1}{2} = \frac{16 - 5}{10} = \frac{11}{10} > 1 \text{ diverge payments}$$

$$\text{Post}$$

$$\text{Test}$$

$$(1.5) \sum_{k=2}^{\infty} \frac{7k}{k^3 + 17}$$

$$\frac{7k}{k^3 + 17} < \frac{7k}{k^3} = \frac{7}{k^2}$$

$$\sum_{k=2}^{2} conveys (P>1)$$

$$\Rightarrow C manze (2t) ... converse$$

(1.6)
$$\sum_{k=0}^{\infty} \frac{5^{3k}}{(2k)!}$$
ratu: $\frac{5^{3(k+1)}}{(3(k+1))!} \cdot \frac{(3k)!}{5^{3k}}$

$$= \frac{5^{3k} \cdot 5^{3}}{(2k+2)(2k+1)(2k)!} \cdot \frac{2k!}{5^{3k}} = \frac{5^{3}}{(2k+2)(2k+1)} \rightarrow 0 < 1$$
 converge by ratio test

$$(1.7) \sum_{k=1}^{\infty} \sin\left(\frac{1}{k}\right)$$

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Assume I an converge. Thus, I an = lings = L (and lim Sn., = L too)

Recall,
$$a_n = S_n - S_{n-1}$$

 $\lim_{n \to \infty} a_n = \lim_{n \to \infty} - S_{n-1} = \emptyset$

2. Prove the following statement: If $\sum a_n$ converges, then $\lim_{n\to+\infty} a_n = 0$

3. Find the value of the convergent series below:

$$(3.1) \sum_{k=1}^{+\infty} \frac{2^{k+1}}{3^{k-1}} = \frac{2 \cdot 2^{k}}{3^{-1} 3^{k}} = 4 \cdot (\frac{2}{3})^{k} = \frac{6}{1/3} = 18$$

$$(3.2) \sum_{k=2}^{+\infty} \left[64^{1/k} - 64^{1/(k+2)} \right]$$

$$S_{2} = \left[64^{1/2} - 64^{1/4} + 64^{1/3} - 64^{1/5} \right]$$

$$S_{3} = \left[64^{1/2} - 64^{1/4} + 64^{1/3} - 64^{1/5} \right]$$

$$S_{4} = \left[64^{1/2} - 64^{1/4} + 64^{1/3} - 64^{1/5} \right] + 64^{1/4} - 64^{1/6} = \left[64^{1/2} + 64^{1/3} - 64^{1/5} - 64^{1/5} \right]$$

$$S_{5} = \left[64^{1/2} + 64^{1/3} - 64^{1/5} - 64^{1/6} \right] + \left[64^{1/3} - 64^{1/7} \right] + \left[64^{1/3} - 64^{1/5} - 64^{1/5} \right]$$

$$S_{6} = \left[64^{1/2} + 64^{1/3} - 64^{1/5} - 64^{1/6} \right] + \left[64^{1/3} - 64^{1/5} - 64^{1/5} \right]$$

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$$S_{7} = \left[64^{1/2} + 64^{1/3} - 64^{1/5} - 64^{1/5} \right]$$

$$S_{8} = \left[64^{1/2} + 64^{1/3} - 64^{1/5} - 64^{1/5} \right]$$

$$S_{1} = \left[64^{1/2} + 64^{1/3} - 64^{1/5} - 64^{1/5} \right]$$

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$$S_{1} = \left[64^{1/$$

- 4. Give three examples (each) of . . .
 - (4.1) a divergent alternating series

(4.2) a conditionally convergent alternating series.

(4.3) an absolutely convergent alternating series

(4.4) a decreasing sequence that converges to $\ln 7$.

(4.5) a strictly increasing sequence that converges to e.

$$\{e - \frac{k}{n}\}$$
 $k = 1, 2, 3$

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$$\{\frac{n}{n+1}\cdot e\}_{n=1}^{\infty}$$

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